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# **”A Production-based Economic Explanation for the Gross Pro tability Premium”**

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Swedish House of Finance Conference on  
Financial Markets and Corporate Decisions  
August 19-20, 2019

# A Production-based Economic Explanation for the Gross Profitability Premium

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- Recent studies document that firms with high gross profitability earn higher returns than low profitability firms (Novy-Marx, 2013);
- This finding has a substantial impact on asset pricing research and motivated the inclusion of the profitability premium as a pricing factor (Hou, Xue, and Zhang, 2015, Fama and French, 2015);
- More profitable firms look more like growth firms (low BM) and less profitable firms look more like value firms (high BM), contradicting the well-established value premium.

In this paper, we provide a production-based explanation for the gross profitability premium:

- A novel hedging effect from intermediate inputs (variable costs):

$$\text{Gross Profitability (GP/A)} = \frac{\text{Revenue} - \text{Variable Cost}}{\text{Total Asset}}$$

- Empirically, both price and cost of intermediate inputs are more procyclical than those of the revenues;
- On average, intermediate inputs offer a hedge to business cycle variations;
- In the cross section, more profitable firms have higher revenue-to-variable-cost ratio and lower hedging effect, leading to a positive gross profitability premium.

# Main contribution

We illustrate this mechanism in a static production-based asset pricing model;

- CES production function between capital and intermediate inputs;
- Production subject to aggregate demand shocks and idiosyncratic productivity shocks;
- Analytically, a positive gross profitability premium when
  - 1 Elasticity of substitution b/t capital and intermediate inputs is low;
  - 2 Price is more procyclical for intermediate inputs than output;

A dynamic extension of the model with capital accumulation and investment-specific technology shocks quantitatively generates:

- Gross profitability premium of about 3.1% (3.69% in the data) and value premium about 3.4% (5.43% in the data);
- A negative correlation of  $-0.27$  ( $-0.5$  in the data) between gross profitability premium and value premium;
- Gross profitability being the other side of value;
- Failure of the unconditional CAPM.

- Explanations for the profitability premium
  - Risk-based explanations:
    - Kogan and Papanikolaou (2013), Ma and Yan (2015)
  - Behavioral explanations:
    - Wang and Yu (2015), Lam, Wang, and Wei (2014), Bouchaud, Krueger, Landier, and Thesmar (2016)
- Explanations for the value premium
  - Berk, Green, Naik (1999), Zhang (2005), Carlson, Fisher, and Giammarino (2004), Cooper (2006), Lettau and Wachter (2007), Kogan and Papanikolaou (2014), Choi (2013), Donangelo (2018), etc.
- Operating leverage
  - Novy-Marx (2010), Carlson, Fisher, and Giammarino (2004), Zhang (2005), Favilukis and Lin (2015), Favilukis, Lin, and Zhao (2017), Petrosky-Nadeau, Zhang, Kuhlen (2018), Donangelo, Gourio, Kehrig, and Palacios (2017)

# A static model

- One period problem, only assets in place;
- CES production function, so gross profits  $\pi$  are

$$\pi = \max_E \left\{ X \left[ (ZE)^{\frac{\eta-1}{\eta}} + K^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}} - P \times E \right\}$$

where  $K$  is capital,  $E$  is intermediate inputs,  $P$  is the purchase price of  $E$ ,  $\eta$  is the elasticity of substitution between capital and intermediate inputs,  $X$  represents the aggregate demand, and  $Z$  is the idiosyncratic input-augmenting productivity;

- FOC implies:

$$\text{GP/A} \equiv \frac{\pi}{K} = X \left[ \left( \frac{ZE}{K} \right)^{\frac{\eta-1}{\eta}} + 1 \right]^{\frac{1}{\eta-1}}$$

$\Rightarrow$  GP/A increases with  $Z$ .

- The exposure of gross profit ( $\pi$ ) to  $X$  shocks:

$$\beta_X \equiv \frac{\partial \log \pi}{\partial \log X} = \frac{\partial \log P}{\partial \log X} + \left(1 - \frac{\partial \log P}{\partial \log X}\right) \left[ \left(\frac{ZE}{K}\right)^{\frac{\eta-1}{\eta}} + 1 \right]$$

- It can be shown:

$$\frac{\partial \beta_X}{\partial \log Z} = (\eta - 1) \left(1 - \frac{\partial \log P}{\partial \log X}\right) \left(\frac{ZE}{K}\right)^{\frac{\eta-1}{\eta}} \left[1 + \left(\frac{ZE}{K}\right)^{\frac{\eta-1}{\eta}}\right].$$

⇒ A positive gross profitability premium if

- 1  $\eta > 1$  and  $\frac{\partial \log P}{\partial \log X} < 1$ ; or
- 2  $\eta < 1$  and  $\frac{\partial \log P}{\partial \log X} > 1$ .



$$\begin{aligned}\text{Gross profit} &= \text{Rev} - \text{COGS} \\ &= \left\{ X \left[ (ZE^*)^{\frac{\eta-1}{\eta}} + K^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}} - P \times E^* \right\}\end{aligned}$$

- When  $\frac{\partial \log P}{\partial \log X} > 1$ ,  $\beta_X(\text{Rev}) < \beta_X(\text{COGS})$ ;
- On average, variable cost generates a hedging effect to  $X$  shocks;
- Cross-sectional heterogeneity: when  $\eta < 1$ ,  $E$  is “sticky”, revenue increases more than variable cost in response to a positive  $Z$  shock;
- High  $Z$  (more profitable) firms have higher Rev/COGS ratio, and less affected by the hedging effect than low  $Z$  (less profitable) firms;
- High  $Z$  firms have higher exposures to  $X$  shocks and higher expected returns than low  $Z$  firms;

⇒ Positive gross profitability premium.

# Aggregate demand elasticity of input price and quantity

Panel A: Summary statistics

	$\Delta P(\text{Output})$	$\Delta P(\text{Input})$	$\Delta Q(\text{Output})$	$\Delta Q(\text{Input})$
Mean (%)	3.35	3.34	3.07	3.03
Std (%)	<b>2.83</b>	<b>3.68</b>	2.81	3.86

Panel B: Elasticity of intermediate input price and quantity w.r.t. output prices

	$\Delta P(\text{Input})$	$\Delta Q(\text{Input})$
$\beta(\Delta P(\text{Output}))$	<b>1.27</b>	-0.27
$t$ -stat	<b>(25.43)</b>	(-1.40)

\*Data from BEA GDP-by-industry account, 1947-2014

- Input price is highly procyclical ( $\frac{\partial \log P}{\partial \log X} > 1$ );
- Input quantity is “sticky” ( $\eta < 1$ ).

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- Input price is highly procyclical ( $\frac{\partial \log P}{\partial \log X} > 1$ );
- Input quantity is “sticky” ( $\eta < 1$ ).

# Estimates of $\eta$

Model predicts:  $GP/A = X \left(\frac{1}{GM}\right)^{\frac{1}{\eta-1}}$ ,  $\eta$  can be estimated from FMB regression:

$$\log GM_{it} = a_t + (1 - \eta_t) \times \log GP/A_{it} + \epsilon_{it}$$

	10 GP/A	10 BM	10 GP/A + 10 BM
$\eta$	<b>0.612</b>	<b>0.371</b>	<b>0.573</b>
se	0.031	0.035	0.025

Industry	$\eta$	se
Agriculture, forestry, fishing, and hunting	0.738	0.037
Arts, entertainment, recreation, etc	0.708	0.032
Construction	0.751	0.037
Educational services, health care, and social assistance	0.510	0.026
Finance, insurance, real estate, rental, and leasing	0.878	0.027
Information	0.642	0.008
Manufacturing	0.534	0.020
Mining	0.690	0.031
Other services, except government	0.733	0.032
Professional and business services	0.607	0.023
Retail trade	0.624	0.021
Transportation and warehousing	0.696	0.046
Utilities	0.743	0.067
Wholesale trade	0.627	0.035

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# Additional implications

When  $\frac{\partial \log P}{\partial \log X} > 1$  and  $\eta < 1$ , firms' responses to an aggregate demand shock and an idiosyncratic productivity shock are very different:

- A positive aggregate demand shock  $\Rightarrow$  Rev  $\uparrow$  and COGS  $\uparrow\uparrow$

**Prediction 1:** At aggregate level,  $\text{Vol}(\text{Rev}) > \text{Vol}(\text{GP})$

- A positive idiosyncratic shock  $\Rightarrow$  Rev  $\uparrow\uparrow$  and COGS  $\uparrow$

**Prediction 2:** At firm level,  $\text{Vol}(\text{Rev}) < \text{Vol}(\text{GP})$

# Sales growth and gross profits growth

Panel A: Sales growth and gross profits growth at the aggregate level

Panel A1			Panel A2	
Summary	$\Delta$ ASale	$\Delta$ AGP	Cyclicality of AGP	
Mean (%)	3.16	3.31	<i>b</i>	0.75
Std (%)	5.75	4.99	<i>t</i> -stat	(14.27)

Panel B: Sales growth and gross profits growth at the firm level

Panel B1			Panel B2	
Summary	$\Delta$ Sale	$\Delta$ GP	Cyclicality of GP	
Mean (%)	7.49	7.06	<i>b</i>	1.14
Std (%)	21.07	26.73	<i>t</i> -stat	(17.73)

⇒ The opposite patterns in responses to aggregate and idiosyncratic shocks are key for the GP/A premium.

# Sales growth and gross profits growth

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Panel B: Sales growth and gross profits growth at the firm level

Panel B1			Panel B2	
Summary	$\Delta$ Sale	$\Delta$ GP	Cyclicality of GP	
Mean (%)	7.49	7.06	<i>b</i>	<b>1.14</b>
Std (%)	<b>21.07</b>	<b>26.73</b>	<i>t</i> -stat	<b>(17.73)</b>

⇒ The opposite patterns in responses to aggregate and idiosyncratic shocks are key for the GP/A premium.



# A dynamic extension: Motivation

- The static model describes the intuition for the gross profitability premium in a parsimonious way;
- But it implies that high  $Z$  firms have high  $V$  and high  $\beta_X$   
 $\Rightarrow$  A negative value premium!!
- Furthermore, one-factor model structure implies CAPM holds;
- We provide a dynamic extension of the model to quantitatively explain both gross profitability premium and value premium.

# A dynamic extension: Setup

- The basic production unit is projects. Each project uses one unit of capital and  $E_{jt}$  units of intermediate inputs;

$$\begin{aligned}\pi_{jt} &= \max_{E_{jt}} \left\{ X_t \left[ (Z_{jt} E_{jt} Y_t)^{\frac{\eta-1}{\eta}} + Y_t^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}} - P_t Y_t E_{jt} \right\} \\ &= Y_t \max_{E_{jt}} \left\{ X_t \left[ (Z_{jt} E_{jt})^{\frac{\eta-1}{\eta}} + 1 \right]^{\frac{\eta}{\eta-1}} - P_t E_{jt} \right\}\end{aligned}$$

where  $Y_t$  is aggregate productivity shock;

- Capital accumulation:

$$K_{jt+1} = (1 - \delta)K_{jt} + \delta S_t A_{jt} K_{jt},$$

where  $K_{jt}$  is the number of projects,  $S_t$  and  $A_{jt}$  measure the aggregate and firm-specific intensity of new project arrivals.

# A dynamic extension: Setup

- Firm value can be written recursively as:

$$V_{jt} = K_{jt}\pi_{jt} + E_t[M_{t+1}V_{jt+1}]$$

subject to profit-maximizing condition and law of motion for capital

- Exogenous processes:

$$x_{t+1} = \rho_x x_t + (1 - \rho_x)\bar{x} + \sigma_x \epsilon_{t+1}^x$$

$$s_{t+1} = \rho_s s_t + (1 - \rho_s)\bar{s} + \sigma_s \epsilon_{t+1}^s$$

$$\Delta y_{t+1} = \sigma_y \epsilon_{t+1}^y$$

$$\log P_t = \log p_0 + \rho_1 \log X_t,$$

$$z_{jt+1} = \rho_z z_{jt} + (1 - \rho_z)\bar{z} + \sigma_z \epsilon_{jt+1}^z + \mu_z$$

$$a_{jt+1} = \rho_a a_{jt} + \sigma_a \epsilon_{jt+1}^a$$

$$\rho_{az} \equiv \text{Corr}(\epsilon_{jt+1}^z, \epsilon_{jt+1}^a) > 0$$

- Pricing kernel:

$$M_{t+1} = \exp\left(-r_f - \gamma_x \sigma_x \epsilon_{t+1}^x - \gamma_y \sigma_y \epsilon_{t+1}^y - \gamma_s \sigma_s \epsilon_{t+1}^s - \frac{1}{2} \gamma_x^2 \sigma_x^2 - \frac{1}{2} \gamma_y^2 \sigma_y^2 - \frac{1}{2} \gamma_s^2 \sigma_s^2\right)$$

# A dynamic extension: Calibration

Parameter	Description	Value
$\gamma_x$	Price of risk for aggregate demand shocks	15
$\gamma_y$	Price of risk for aggregate productivity shocks	6.5
$\gamma_s$	Price of risk for aggregate investment shocks	-10
$\eta$	Elasticity of substitution between capital and inputs	0.3
$\delta$	Depreciation rate	0.01
$r_f$	Risk-free rate	0.25%
$\bar{x}$	Unconditional aggregate demand	0
$\rho_x$	Persistence of aggregate demand shocks	0.98
$\sigma_x$	Conditional volatility of aggregate demand shocks	0.04
$\sigma_y$	Conditional volatility of aggregate productivity shocks	0.027
$\bar{s}$	Unconditional aggregate investment opportunity	-0.146
$\rho_s$	Persistence of aggregate investment shocks	0.9685
$\sigma_s$	Conditional volatility of aggregate investment shocks	0.026
$\bar{z}$	Unconditional idiosyncratic productivity	1.1
$\rho_z$	Persistence of idiosyncratic productivity shocks	0.97
$\sigma_z$	Conditional volatility of idiosyncratic productivity shocks	0.075
$\rho_a$	Persistence of idiosyncratic investment shocks	0.98
$\sigma_a$	Conditional volatility of idiosyncratic investment shocks	0.107
$\rho_{az}$	Correlation between $z$ shocks and $a$ shocks	0.18
$p_0$	Logarithm of the level of intermediate inputs price	0.588
$p_1$	Cyclicality of intermediate inputs price w.r.t. aggregate demand	1.39
$\phi$	Leverage ratio	1.67

# A dynamic extension: Moments

Moment	Data	Model
Average annual aggregate GP/A	0.24	0.25
AR(1) of aggregate annual GP/A	0.87	0.92
Average book-to-market ratio	0.53	0.44
AR(1) of aggregate book-to-market	0.89	0.89
Average annual aggregate investment rate	11.4%	11.1%
Standard deviation of annual aggregate investment rate	1%	1%
AR(1) of annual aggregate investment rate	0.73	0.72
Average aggregate sales - aggregate variable costs ratio	1.44	1.50
Vol. of agg. sales - agg. variable costs ratio	0.05	0.05
Vol. of agg. variable costs growth/vol. of agg. sales growth	1.12	1.15
Corr. b/w agg. sales growth and agg. variable costs growth	0.99	0.99
Vol. of firm variable costs growth/Vol. of firm sales growth	0.99	0.91
Value-weighted annual market premium	6.47%	8.87%
Value-weighted annual market volatility	16.96%	18.33%
Equally-weighted annual market premium	10.9%	9.42%
Equally-weighted annual market volatility	26.03%	18.13%
Volatility of monthly firm-level stock returns	12.6%	10.9%

# A dynamic extension: Portfolio characteristics

	GP/A portfolios				
	GP/A	logBM	GM	Z	A
Lo	0.05	-0.93	0.09	0.71	-0.36
2	0.16	-1.02	0.23	0.95	-0.28
3	0.24	-1.09	0.30	1.10	-0.23
4	0.33	-1.14	0.37	1.25	-0.18
Hi	0.47	-1.24	0.47	1.49	-0.10

	Book-to-market portfolios				
	GP/A	logBM	GM	Z	A
Lo	0.31	-1.56	0.35	1.24	0.52
2	0.29	-1.21	0.33	1.19	0.04
3	0.26	-1.05	0.31	1.13	-0.24
4	0.23	-0.90	0.28	1.05	-0.52
Hi	0.16	-0.70	0.21	0.89	-0.94

- Gross margin is higher for High GP/A and growth stocks;
- Gross profitability looks like the other side of value;
- GP/A portfolios mainly sorts on Z; BM portfolios mainly sorts on A.

# A dynamic extension: Portfolio returns and AP tests

GP/A portfolios						
	Lo	2	3	4	Hi	Hi-Lo
Mean	6.87	7.74	8.39	9.09	10.00	3.13
Std	16.95	17.08	17.15	17.23	17.45	5.59
$\alpha$	-1.52	-0.72	-0.11	0.56	1.36	2.88
	(-3.15)	(-1.51)	(-0.23)	(1.15)	(2.77)	(3.67)
MKT	0.99	0.99	1.00	1.00	1.01	0.03
$\alpha$	-2.00	-0.92	-0.17	0.68	1.79	3.79
	(-4.11)	(-1.89)	(-0.35)	(1.34)	(3.58)	(4.84)
MKT	1.00	1.00	1.00	1.00	1.00	0.00
HML	0.11	0.05	0.01	-0.03	-0.10	-0.20

Book-to-market portfolios						
	Lo	2	3	4	Hi	Hi-Lo
Mean	6.45	8.78	9.42	9.89	9.86	3.40
Std	18.46	17.01	16.67	16.42	16.18	7.32
$\alpha$	-2.64	0.31	1.12	1.73	1.86	4.50
	(-4.50)	(0.76)	(2.80)	(4.07)	(3.90)	(4.59)
MKT	1.07	1.00	0.97	0.96	0.94	-0.13
$\alpha$	-0.12	-0.26	0.17	0.48	-0.12	0.00
	(-0.56)	(-0.68)	(0.48)	(1.43)	(-0.56)	
MKT	1.00	1.01	1.00	0.99	1.00	0.00
HML	-0.56	0.13	0.21	0.28	0.44	1.00

# A dynamic extension: Portfolio returns and AP tests

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$\alpha$	-1.52 (-3.15)	-0.72 (-1.51)	-0.11 (-0.23)	0.56 (1.15)	1.36 (2.77)	2.88 (3.67)
MKT	0.99	0.99	1.00	1.00	1.01	0.03
$\alpha$	-2.00 (-4.11)	-0.92 (-1.89)	-0.17 (-0.35)	0.68 (1.34)	1.79 (3.58)	3.79 (4.84)
MKT	1.00	1.00	1.00	1.00	1.00	0.00
HML	0.11	0.05	0.01	-0.03	-0.10	-0.20

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Std	18.46	17.01	16.67	16.42	16.18	7.32
$\alpha$	-2.64 (-4.50)	0.31 (0.76)	1.12 (2.80)	1.73 (4.07)	1.86 (3.90)	4.50 (4.59)
MKT	1.07	1.00	0.97	0.96	0.94	-0.13
$\alpha$	-0.12 (-0.56)	-0.26 (-0.68)	0.17 (0.48)	0.48 (1.43)	-0.12 (-0.56)	0.00
MKT	1.00	1.01	1.00	0.99	1.00	0.00
HML	-0.56	0.13	0.21	0.28	0.44	1.00



# A dynamic extension: Portfolio risk exposures

	GP/A portfolios					
	Lo	2	3	4	Hi	Hi-Lo
$\beta(X)$	0.05 (4.99)	0.09 (7.94)	0.11 (10.12)	0.14 (12.39)	0.18 (15.67)	<b>0.13</b> <b>(8.49)</b>
$\beta(Y)$	1.68 (107.99)	1.68 (103.09)	1.68 (101.96)	1.68 (98.46)	1.68 (96.55)	0.00 (0.17)
$\beta(S)$	0.62 (39.01)	0.64 (37.99)	0.65 (37.73)	0.66 (37.39)	0.69 (38.12)	0.06 (2.59)

	Book-to-market Portfolios					
	Lo	2	3	4	Hi	Hi-Lo
$\beta(X)$	0.12 (8.41)	0.13 (14.66)	0.13 (16.63)	0.12 (17.26)	0.09 (14.84)	-0.02 (-1.62)
$\beta(Y)$	1.68 (80.60)	1.68 (126.62)	1.68 (145.28)	1.68 (159.42)	1.68 (179.85)	0.00 (0.21)
$\beta(S)$	0.95 (44.07)	0.65 (47.71)	0.55 (45.94)	0.47 (44.00)	0.38 (39.89)	<b>-0.57</b> <b>(-24.46)</b>

- The GP/A premium loads strongly on aggregate demand ( $X$ ) shocks;
- The value premium loads strongly on investment ( $S$ ) shocks ;
- Portfolio exposures to aggregate productivity ( $Y$ ) shocks are flat;
- A positive  $\rho_{az}$  gives rise to a negative correlation between GP/A premium and value premium.

# A dynamic extension: Portfolio risk exposures

	GP/A portfolios					
	Lo	2	3	4	Hi	Hi-Lo
$\beta(X)$	0.05 (4.99)	0.09 (7.94)	0.11 (10.12)	0.14 (12.39)	0.18 (15.67)	0.13 (8.49)
$\beta(Y)$	<b>1.68</b> (107.99)	<b>1.68</b> (103.09)	<b>1.68</b> (101.96)	<b>1.68</b> (98.46)	<b>1.68</b> (96.55)	<b>0.00</b> (0.17)
$\beta(S)$	0.62 (39.01)	0.64 (37.99)	0.65 (37.73)	0.66 (37.39)	0.69 (38.12)	0.06 (2.59)

	Book-to-market Portfolios					
	Lo	2	3	4	Hi	Hi-Lo
$\beta(X)$	0.12 (8.41)	0.13 (14.66)	0.13 (16.63)	0.12 (17.26)	0.09 (14.84)	-0.02 (-1.62)
$\beta(Y)$	<b>1.68</b> (80.60)	<b>1.68</b> (126.62)	<b>1.68</b> (145.28)	<b>1.68</b> (159.42)	<b>1.68</b> (179.85)	<b>0.00</b> (0.21)
$\beta(S)$	0.95 (44.07)	0.65 (47.71)	0.55 (45.94)	0.47 (44.00)	0.38 (39.89)	-0.57 (-24.46)

- The GP/A premium loads strongly on  $X$  shocks;
- The value premium loads strongly on  $S$  shocks;
- Portfolio exposures to  $Y$  shocks are flat;
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$\beta(X)$	0.05 (4.99)	0.09 (7.94)	0.11 (10.12)	0.14 (12.39)	0.18 (15.67)	<b>0.13</b> <b>(8.49)</b>
$\beta(Y)$	1.68 (107.99)	1.68 (103.09)	1.68 (101.96)	1.68 (98.46)	1.68 (96.55)	0.00 (0.17)
$\beta(S)$	0.62 (39.01)	0.64 (37.99)	0.65 (37.73)	0.66 (37.39)	0.69 (38.12)	<b>0.06</b> <b>(2.59)</b>

	Book-to-market Portfolios					
	Lo	2	3	4	Hi	Hi-Lo
$\beta(X)$	0.12 (8.41)	0.13 (14.66)	0.13 (16.63)	0.12 (17.26)	0.09 (14.84)	<b>-0.02</b> <b>(-1.62)</b>
$\beta(Y)$	1.68 (80.60)	1.68 (126.62)	1.68 (145.28)	1.68 (159.42)	1.68 (179.85)	0.00 (0.21)
$\beta(S)$	0.95 (44.07)	0.65 (47.71)	0.55 (45.94)	0.47 (44.00)	0.38 (39.89)	<b>-0.57</b> <b>(-24.46)</b>

- The GP/A premium loads strongly on  $X$  shocks;
- The value premium loads strongly on  $S$  shocks;
- Portfolio exposures to  $Y$  shocks are flat;
- A positive  $\rho_{az}$  gives rise to a negative correlation between GP/A premium and value premium.

- A production-based explanation for the gross profitability premium;
  - A novel hedging effect from intermediate inputs;
  - More profitable firms have higher exposure to the aggregate demand shock than less profitable firms due to heterogeneity in hedging effect;
- A dynamic extension offers a unified interpretation for gross profitability premium and value premium;
- It reproduces the coexistence of gross profitability premium and value premium, their negative correlation, and the failure of CAPM.